

pH, pKa and Henderson-Hasselbalch Calculations ([corrections 2/5/04](#))

1. Calculate the concentration of benzoic acid and benzoate in a solution whose pH = 5.2. The pKa of benzoic acid is 4.20 and the solution was prepared to be 0.005 M benzoic acid. (Connors, p. 164)

$$\begin{aligned}\text{pH} &= \text{pKa} + \log[\text{A}^-/\text{HA}] \\ 5.20 &= 4.20 + \log[\text{A}^-/\text{HA}] \\ 1.0 &= \log[\text{A}^-/\text{HA}]\end{aligned}$$

**10 = [A⁻]/[HA] → says the concentration of benzoate is ten times that of benzoic acid or the fractional amount is: [A⁻]/([HA] + [A⁻]) or 1/11 [HA] and 10/11 [A⁻].
The fractional amount of [HA] is: 0.005 M x 1/11 = .0004545 M (4.5 x 10⁻⁴ M)
The fractional amount of [A⁻] is: 0.005 M x 10/11 = .004545 M (4.5 x 10⁻³ M)**

2. From class... Calculate the pH of a buffer solution prepared by dissolving 242.2 mg of tris(hydroxymethyl)aminomethane in 10.0 mL of 0.170 M HCl and diluting it to 100 mL with water. The mw of tris = 121.1 and has a pKa = 8.08. Connors p. 170

**Tris: 242.2 mg/121.1 g/mol = 2.00 mmol (or 0.002 M).
HCl: 10 mL x 0.170 M/L = 1.7 mmol or 0.0017 M)**

If 1.7 mmol HCl is added to 2.0 mmol of tris then 1.7 mmol of tris-HCl forms but leaves 0.3 mmol ~~HCl~~ tris unreacted (tris HCl is ~~as~~ the conjugate acid). And....

Note: My narrative error from discussion section is denoted in blue (vs. red strikethrough) above – thanks to those of you who caught it. The numbers are correct.

pH = pKa + log[A⁻/HA] or pH = pKa + log[tris/trisHCl] (tris is equivalent to the ionized A⁻ and trisHCl is equivalent to the acid HA.

$$\text{pH} = 8.08 + \log [0.3/1.7] = 7.32$$

3. Ephedrine (pKa = 9.6) reacts with hydrochloric acid to afford the ephedrine hydrochloride salt. If you react 1 M ephedrine with 1 M HCl what is the pH? (Cairnes p. 22)

The key is to remember is that when you add 1.0 M ephedrine to 1.0 M HCl the result is a 0.5 M solution. For example, adding 10 mL of 1 M ephedrine to 10 mL of 1.0 M HCl gives you 20 mL from the same molarity – but a net dilution of two-fold or 0.5 M. So....

$$\begin{aligned}\text{pH} &= \frac{1}{2}\text{pKa} - \frac{1}{2} \log C \\ &= \frac{1}{2} (9.6) - \frac{1}{2} \log (0.5 \text{ M}) \\ &= 4.8 - (-0.15) \\ &= 4.95\end{aligned}$$

4. What is the pH of 0.05 M sodium acetate given that acetic acid pKa = 4.66. Although sodium acetate is a weak base, we can use the weak acid equation to calculate and then subtract from 14.

Sodium acetate is a weak base so we substitute for pKa using the equation:

$$\text{pKw} = \text{pKa} + \text{pKb} \quad \text{or}$$

$$\text{pKw} - \text{pKb} = \text{pKa}$$

$$\begin{aligned} \text{if } \text{pH} &= \frac{1}{2}\text{pKa} - \frac{1}{2} \log C \\ \text{then } \text{pH} &= \frac{1}{2} (\text{pKw} - \text{pKb}) - \frac{1}{2} \log C \\ &= \frac{1}{2} (14 - 4.66) - \frac{1}{2} \log (0.05 \text{ M}) \\ &= 4.67 - (-0.65) \\ &= 5.32 \end{aligned}$$

and

$$14 - 5.32 = 8.68$$

5. An antilog calculation!! Calculate the concentration of acetic acid needed to be added to a 0.1 M solution of sodium acetate to give a buffer of pH 5 (pKa of acetic acid = 4.66). (Cairns, p. 24)

$$\begin{aligned} \text{pH} &= \text{pKa} + \log[\text{A}^-/\text{HA}] \\ 5.0 &= 4.66 + \log (0.1/\text{HA}) \\ 0.34 &= \log 0.1 - \log[\text{HA}] \\ 1.34 &= -\log[\text{HA}] \\ 0.045 \text{ M} &[\text{acetic acid}] \end{aligned}$$

6. Calculating the fractional amount of a compound in the ionized and unionized forms. Pentobarbitone (pKa 8.0) is a weak acid. Calculate the percentage of a dose of this drug in the plasma (pH 7.4).

First, since the pH is lower than the pKa, the higher proportion of the drug will be unionized!!!

$$\begin{aligned} \text{pH} &= \text{pKa} + \log[\text{A}^-/\text{HA}] \\ 7.4 &= 8.0 + \log[\text{A}^-/\text{HA}] \\ -0.6 &= \log[\text{A}^-/\text{HA}] \\ 0.25 &= \frac{1}{4} = [\text{A}^-]/[\text{HA}] \quad \text{or there are four HA's for every one A}^-. \quad 4 + 1 = 5 \text{ total.} \\ \text{So the fractional amounts are } &4/5 \times 100\% \text{ pHA] and } 1/5 \times 100\% [\text{A}^-] \\ &80\% \text{ pentobarbitone and } 20\% \text{ pentobarbitone anion (conjugate base).} \end{aligned}$$